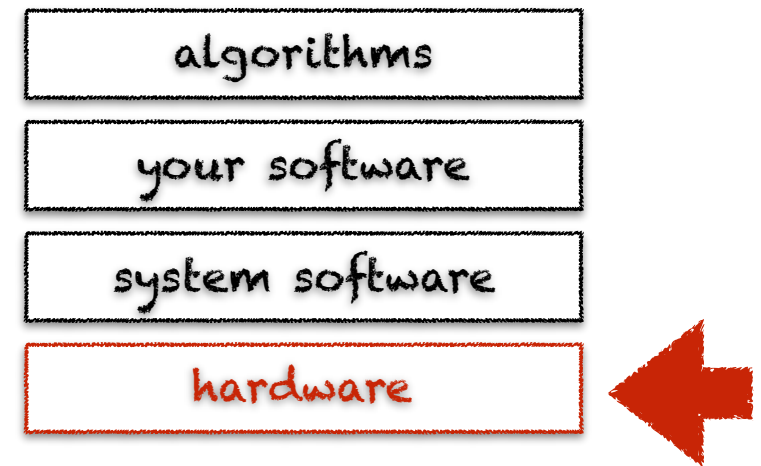


computer architecture

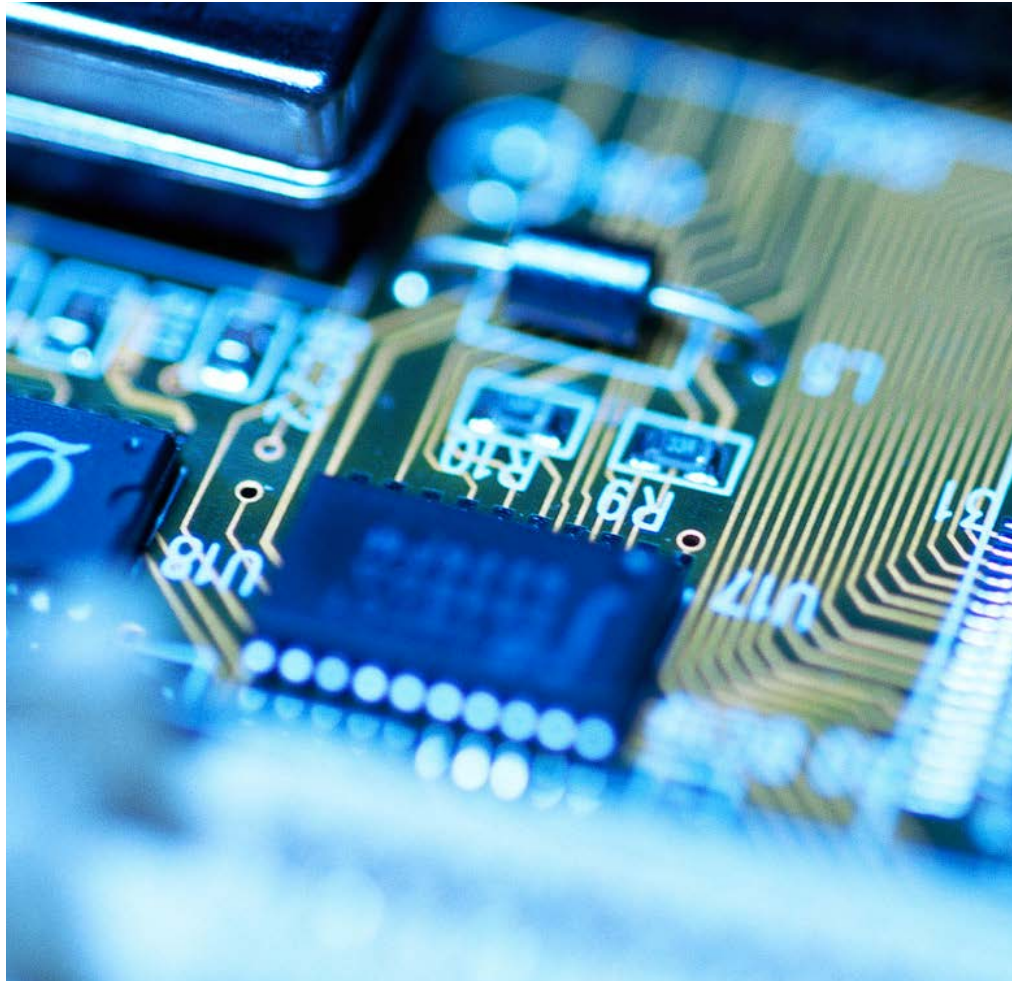


learning objectives



- ♦ understand the basics of how a computer works
- ♦ understand the basics of binary computation
- ♦ learn the basics of the Von Neumann architecture

what's a computer?



hardware

+



software

a dual origin

mathematics

Associative Rules:

Distributive Rules:

Idempotent Rules:

Double Negation:

DeMorgan's Rules:

Commutative Rules:

Absorption Rules:

Bound Rules:

Negation Rules:

$$(p \wedge q) \wedge r \Leftrightarrow p \wedge (q \wedge r)$$

$$p \wedge (q \vee r) \Leftrightarrow (p \wedge q) \vee (p \wedge r)$$

$$p \wedge p \Leftrightarrow p$$

$$\neg \neg p \Leftrightarrow p$$

$$\neg(p \wedge q) \Leftrightarrow \neg p \vee \neg q$$

$$p \wedge q \Leftrightarrow q \wedge p$$

$$p \vee (p \wedge q) \Leftrightarrow p$$

$$p \wedge F \Leftrightarrow F \quad p \wedge T \Leftrightarrow p$$

$$p \wedge (\neg p) \Leftrightarrow F$$

$$(p \vee q) \vee r \Leftrightarrow p \vee (q \vee r)$$

$$p \vee (q \wedge r) \Leftrightarrow (p \vee q) \wedge (p \vee r)$$

$$p \vee p \Leftrightarrow p$$

$$\neg(p \vee q) \Leftrightarrow \neg p \wedge \neg q$$

$$p \vee q \Leftrightarrow q \vee p$$

$$p \wedge (p \vee q) \Leftrightarrow p$$

$$p \vee T \Leftrightarrow T \quad p \vee F \Leftrightarrow p$$

$$p \vee (\neg p) \Leftrightarrow T$$

p	$\neg p$
F	T
T	F

p	q	$p \wedge q$
F	F	F
F	T	F
T	F	F
T	T	T

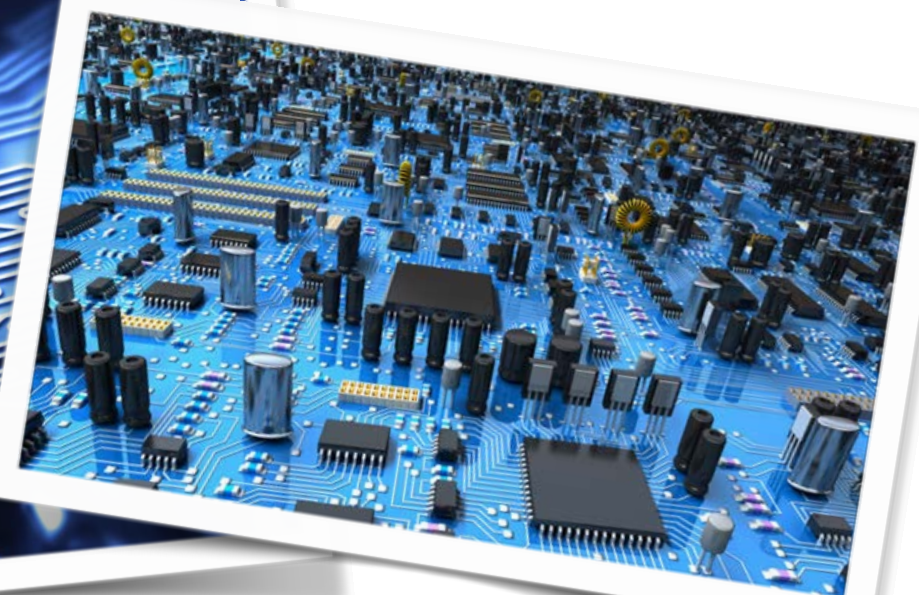
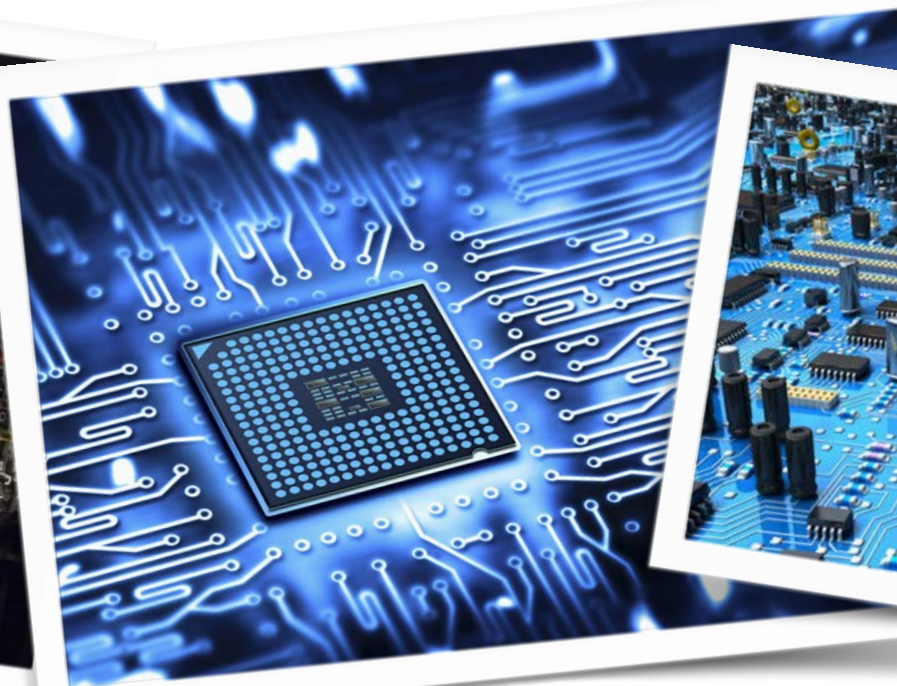
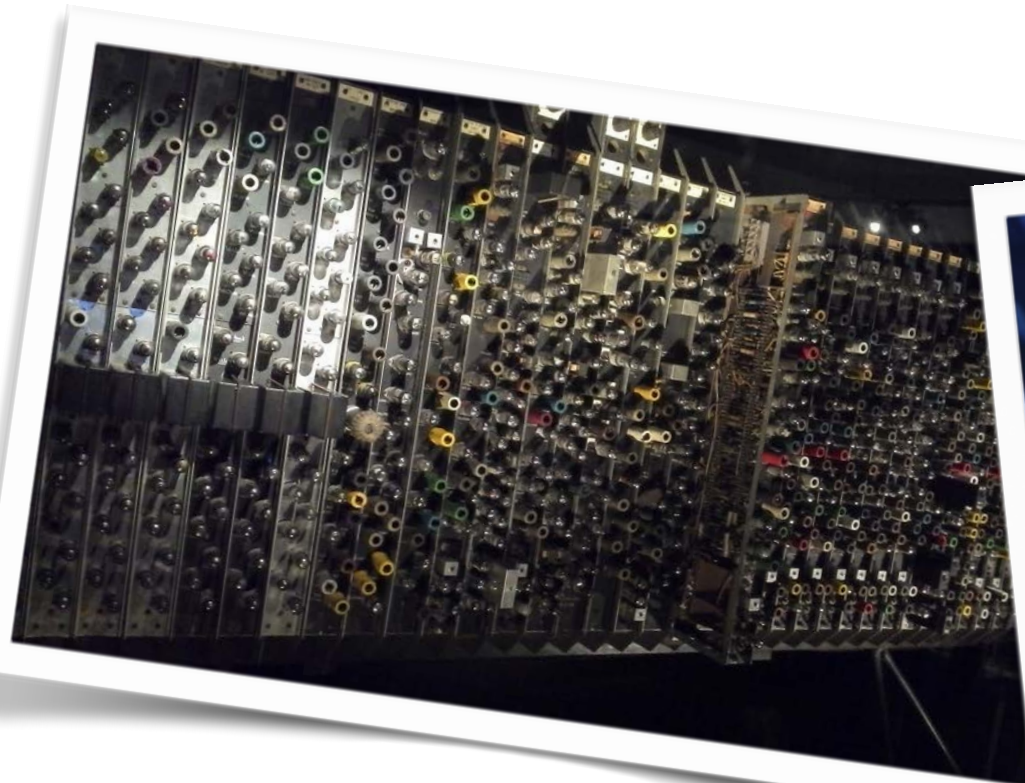
p	q	$p \vee q$
F	F	F
F	T	T
T	F	T
T	T	T

$$\left\{ \frac{2^i - 1}{2^i} \right\}_{i=1}^{\infty} = \frac{1}{2}, \frac{3}{4}, \frac{7}{8}, \frac{15}{16}, \dots,$$

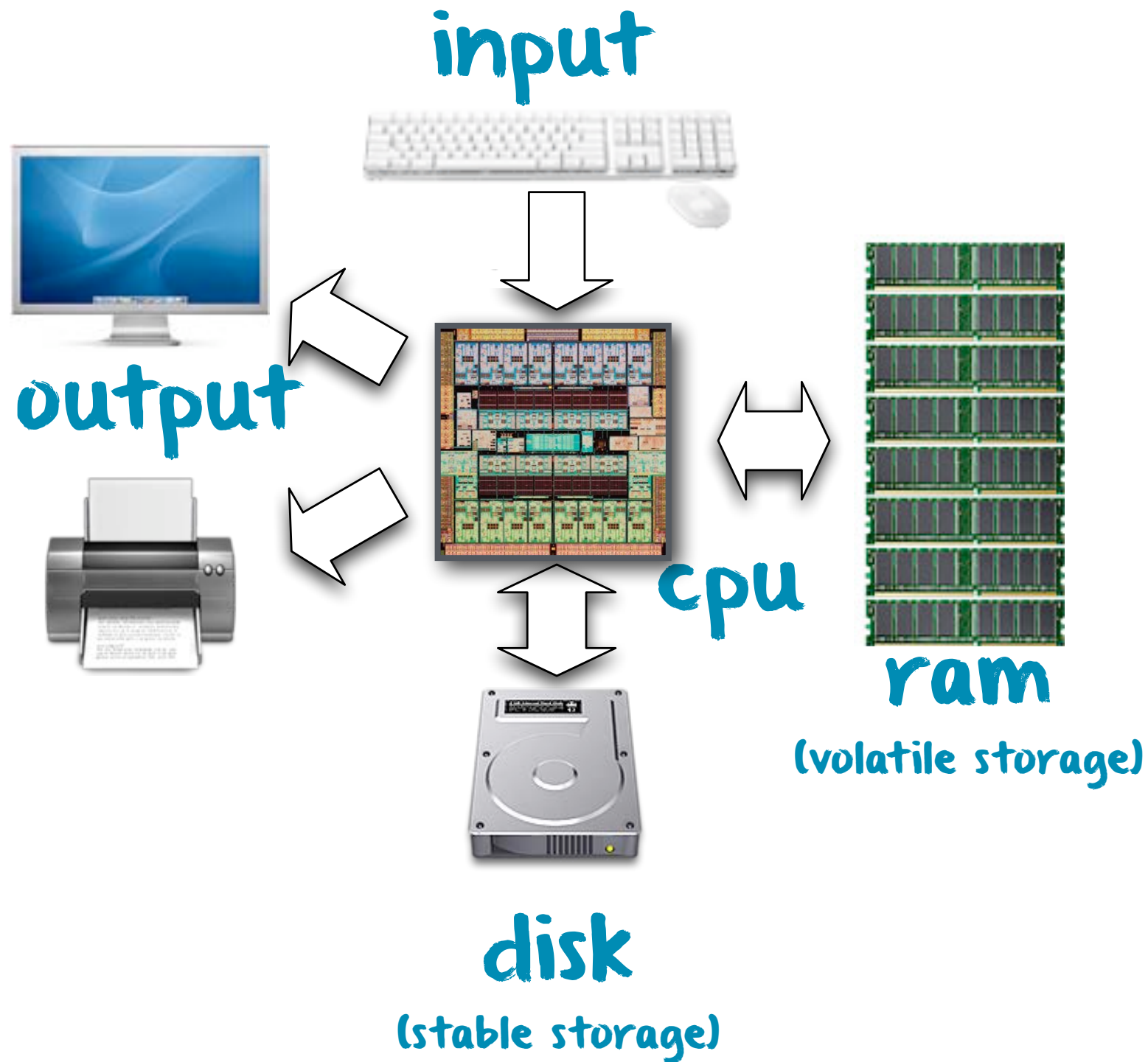
$$\left\{ \frac{n+1}{n} \right\}_{i=1}^{\infty} = \frac{2}{1}, \frac{3}{2}, \frac{4}{3}, \frac{5}{4}, \dots$$

$$\frac{a_{n+1}}{a_n} = \frac{(n+1)!}{(n+1)^{n+1}} \frac{n^n}{n!} = \frac{(n+1)!}{n!} \frac{n^n}{(n+1)^{n+1}} = \frac{n+1}{n+1} \left(\frac{n}{n+1} \right)^n = \left(\frac{n}{n+1} \right)^n < 1.$$

electronics

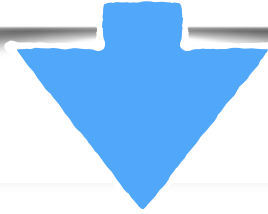


what's hardware?



cpu = central processing unit

what's software?

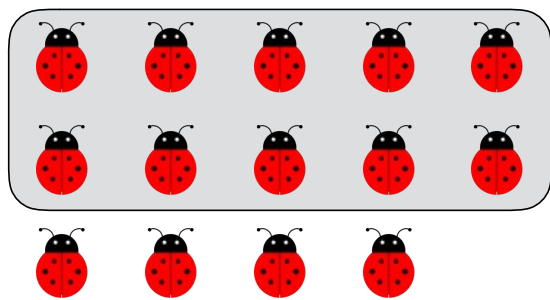
$$i \leftarrow i + 1$$

$$\begin{aligned} i &= 0 \\ i &= i + 1 \end{aligned}$$


```
0010010100101011
0001001010100100
1111001101010011
```

we will come back to these transformations in the next module

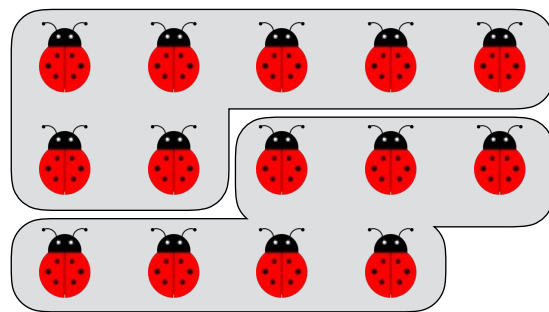
binary computation

base 10



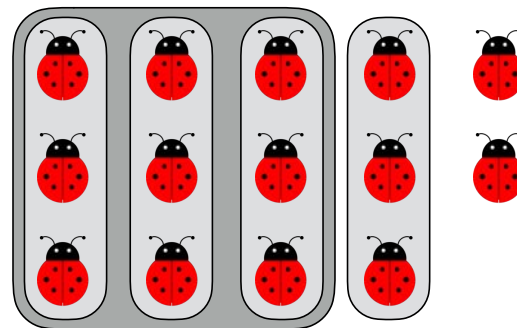
10^2	10^1	10^0
	1	4

base 7



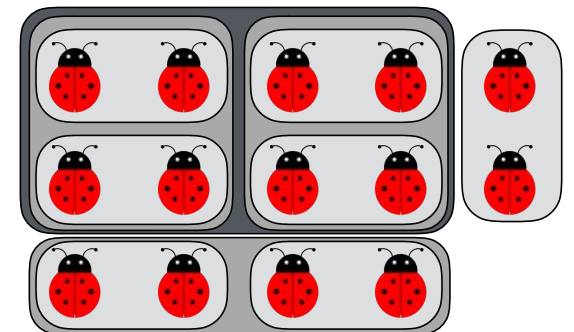
7^2	7^1	7^0
	2	0

base 3



3^2	3^1	3^0
1	1	2

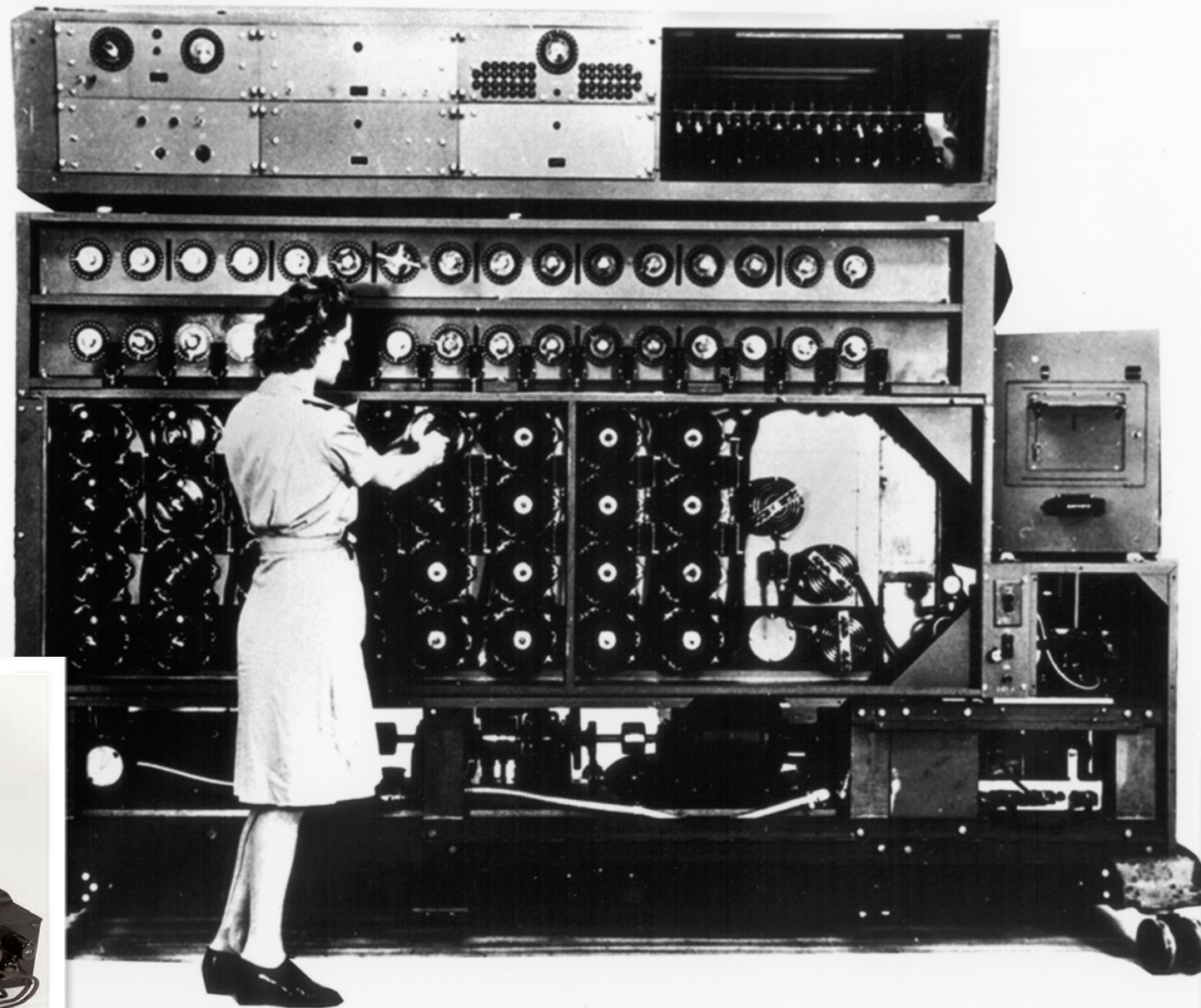
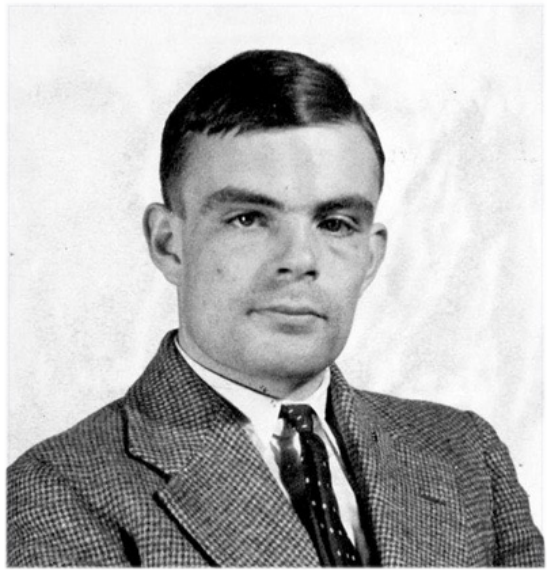
base 2



2^3	2^2	2^1	2^0
1	1	1	0

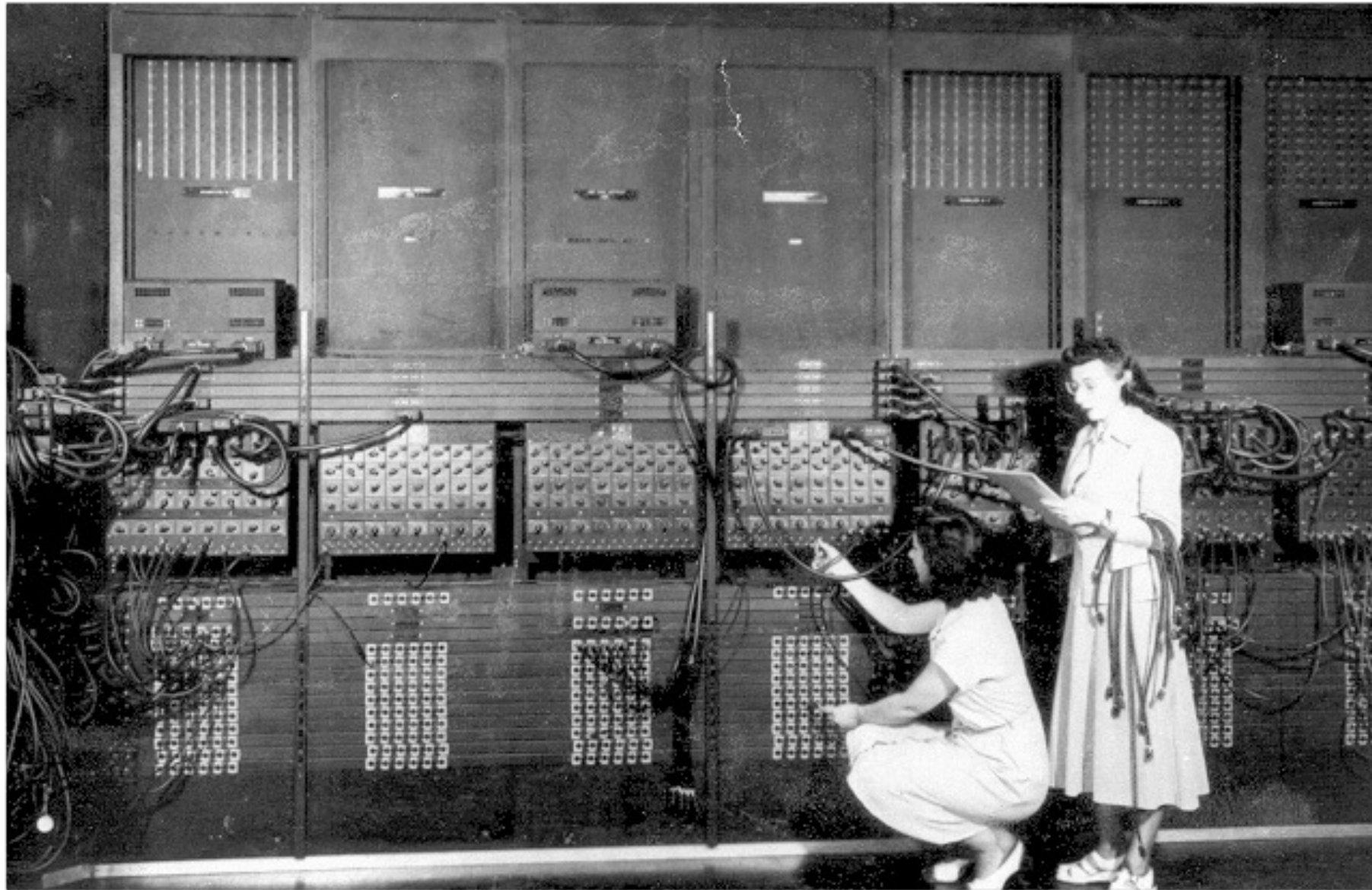
note that in a computer, binary words are not only used to represent integer numbers

1939-40



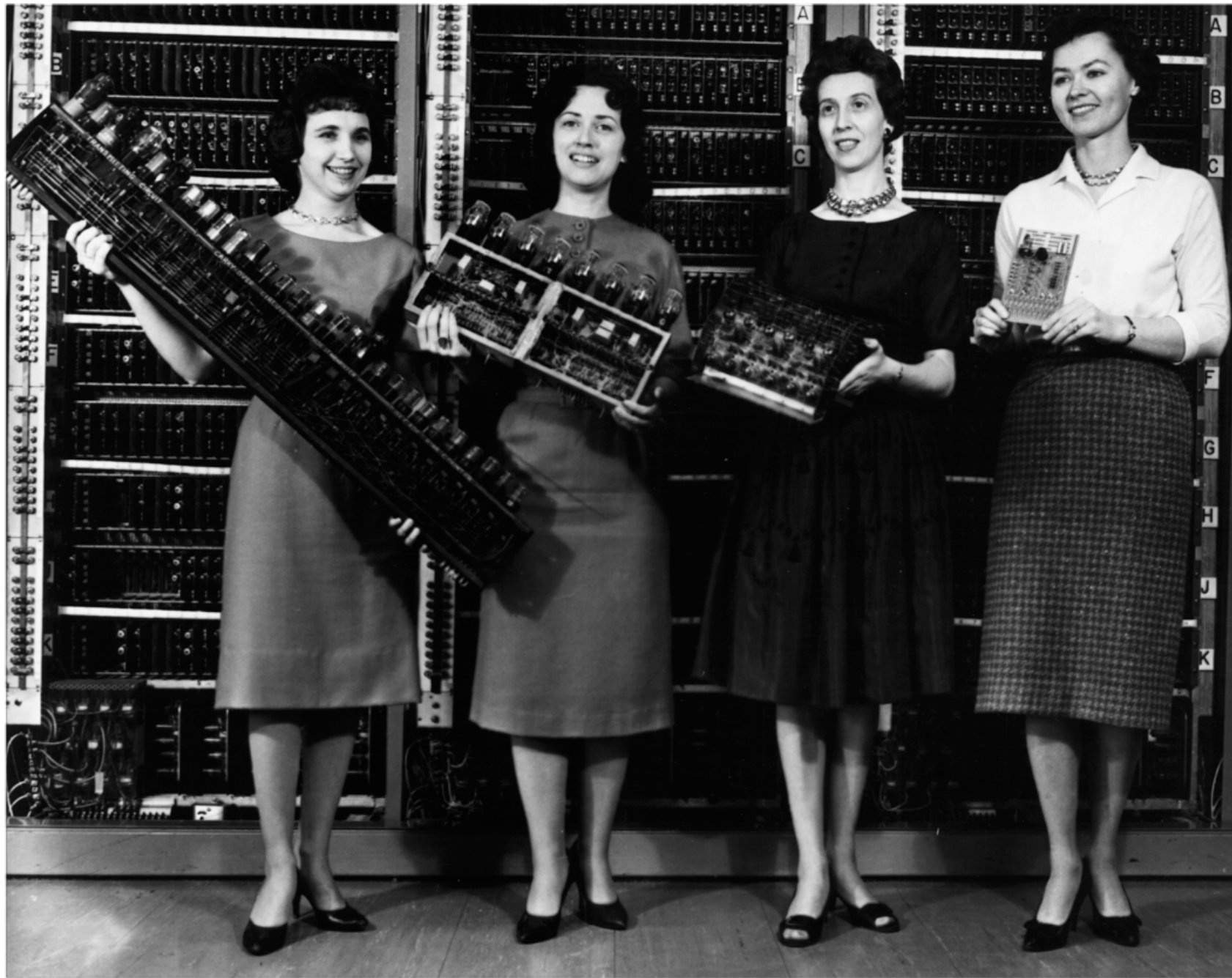
the "bombe" was an electromechanical device designed by Alan Turing to decipher German **Enigma-encrypted** messages

1943



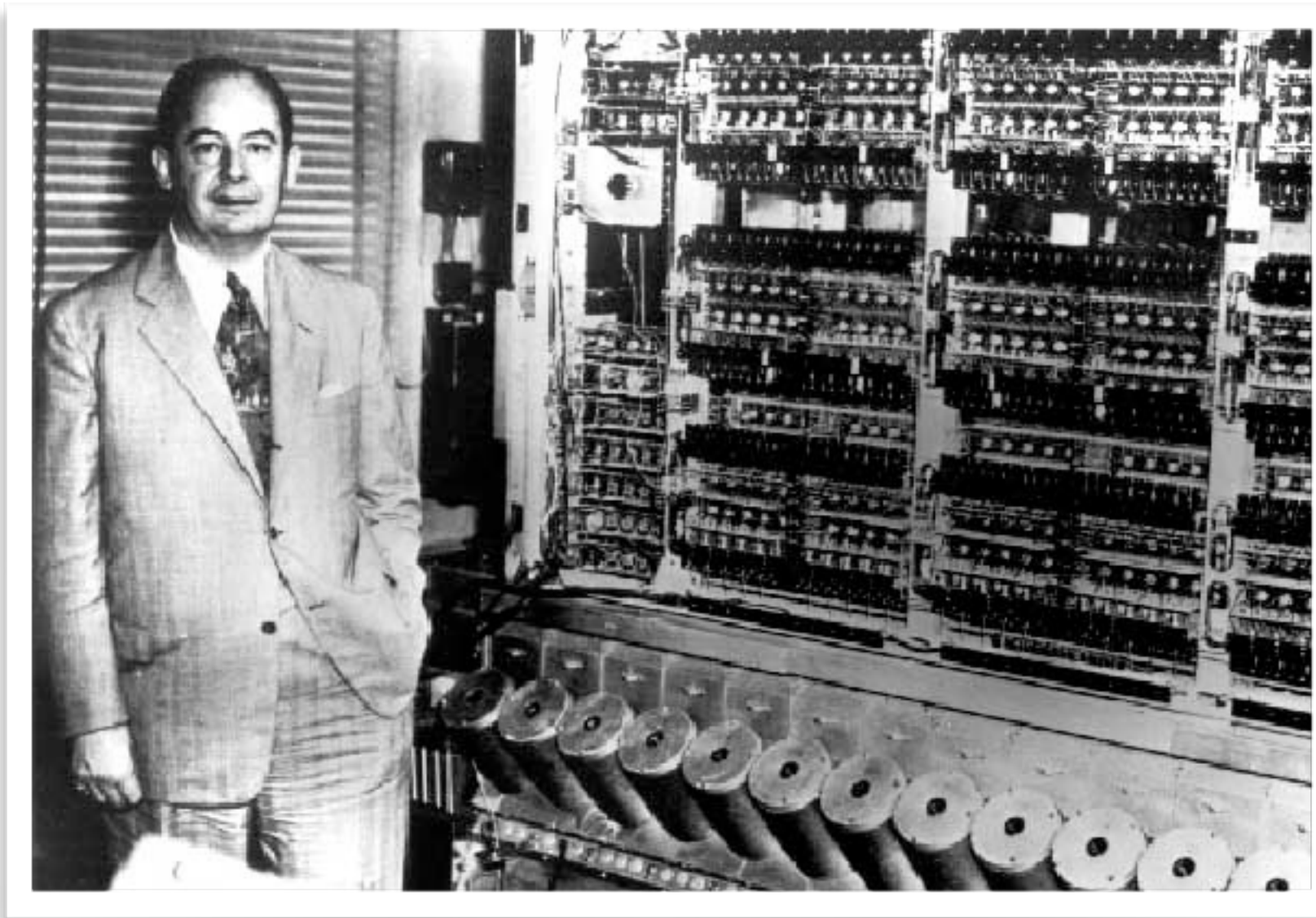
the ENIAC was the first general electronic computer
programs were **hard-wired** (dials & switches)

1944



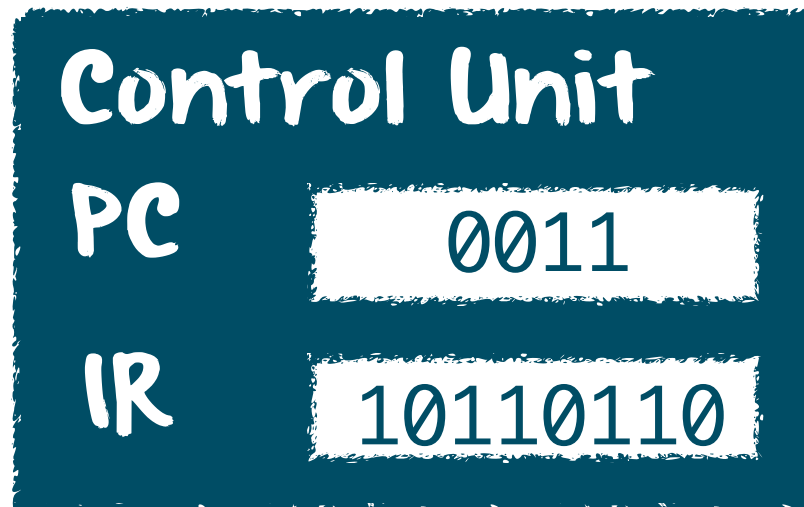
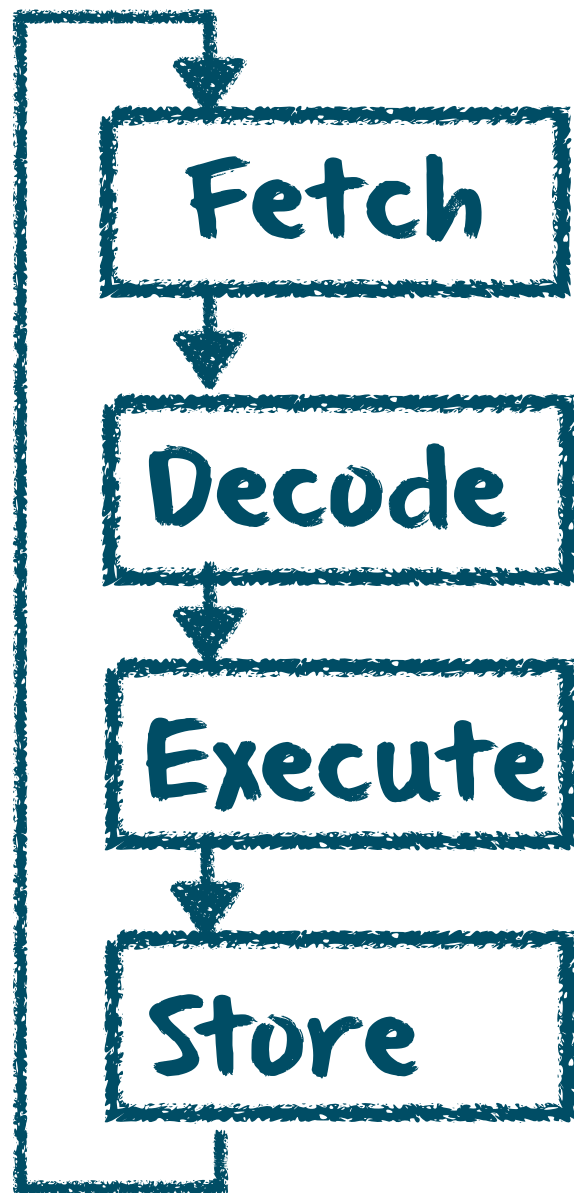
the EDVAC is the first computer to rely on
programs stored in **memory**

1945

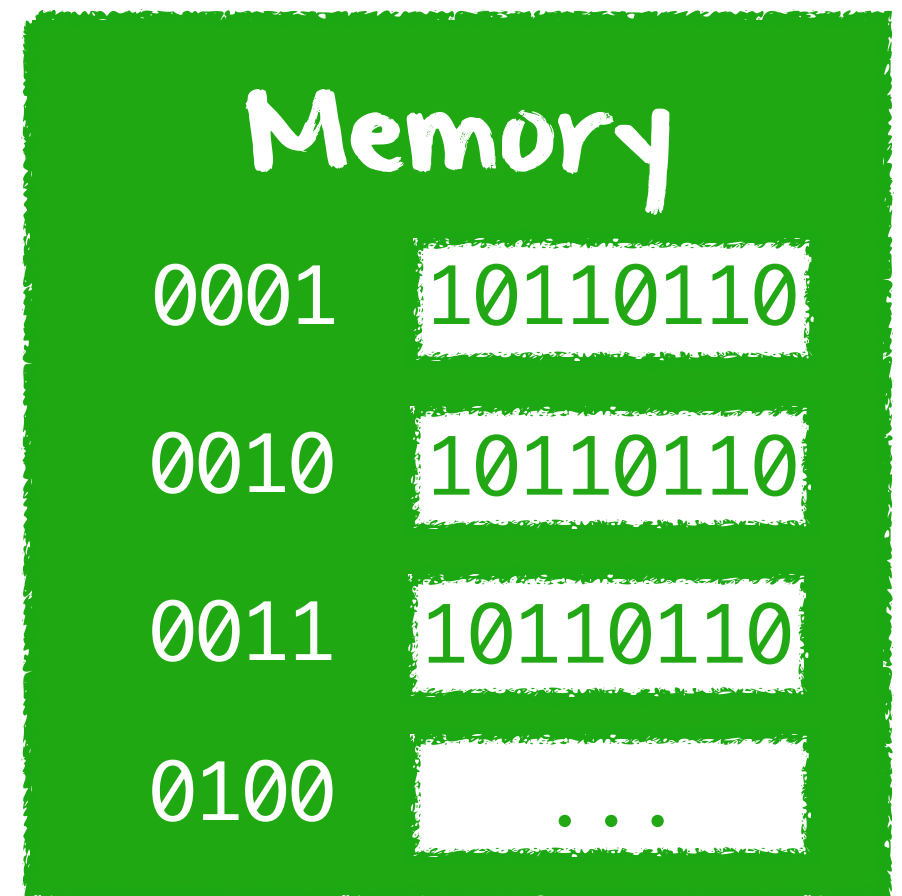
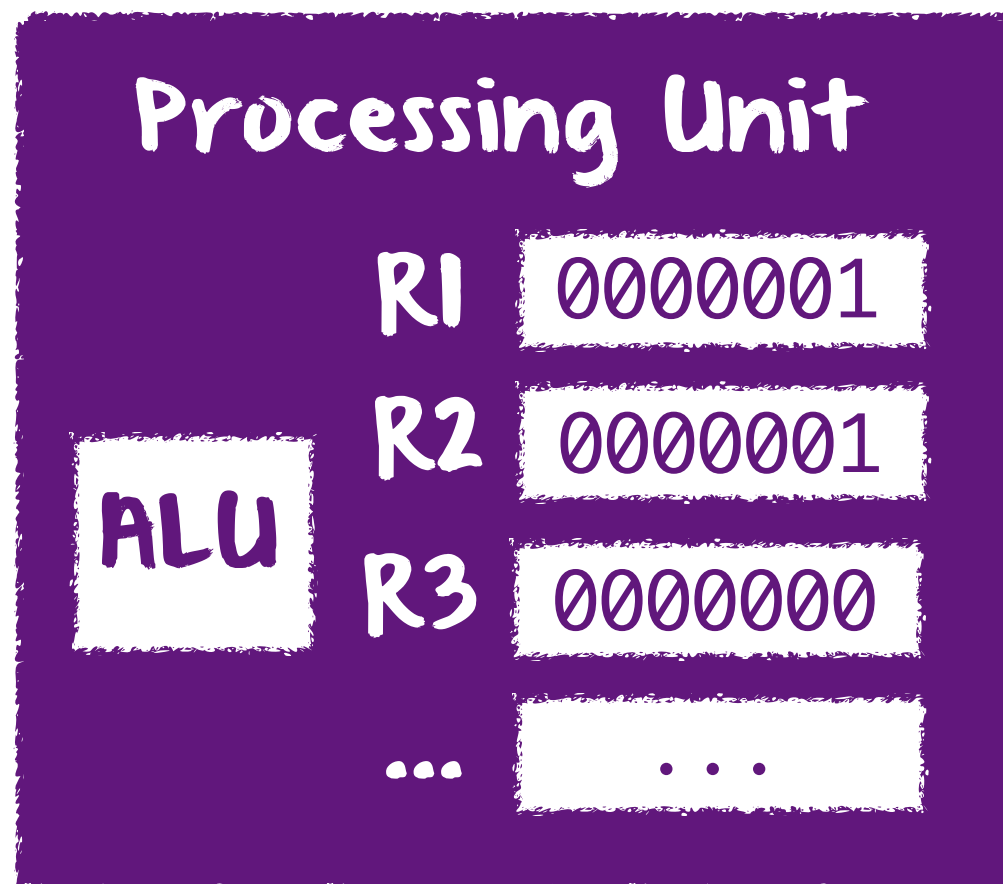


John von Neumann describes the concept of programs stored in memory in a report about the EDVAC computer: **the Von Neumann**

the von Neumann model

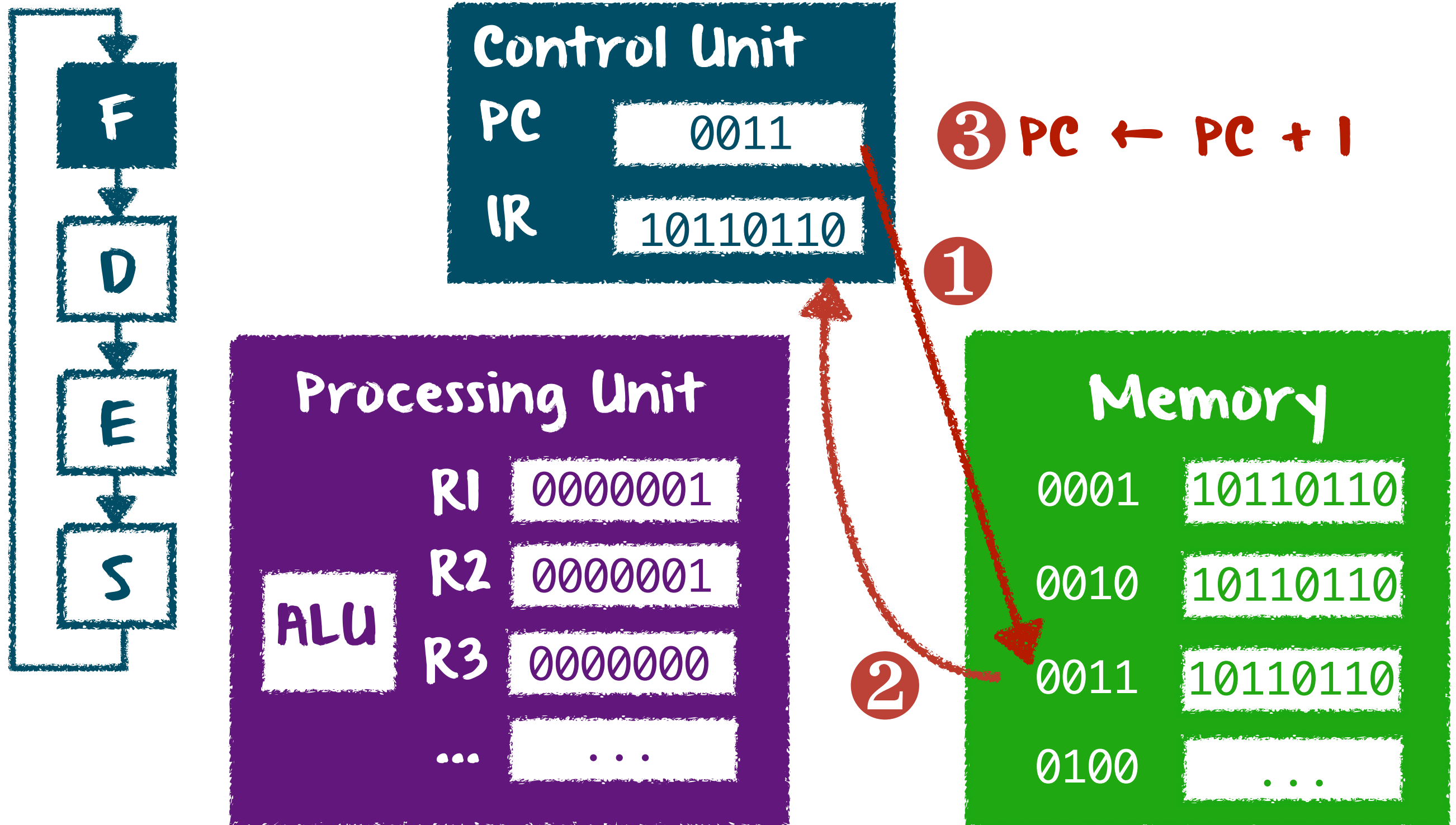


PC: Program Counter
IR: Instruction Register
R1-Rn: Register

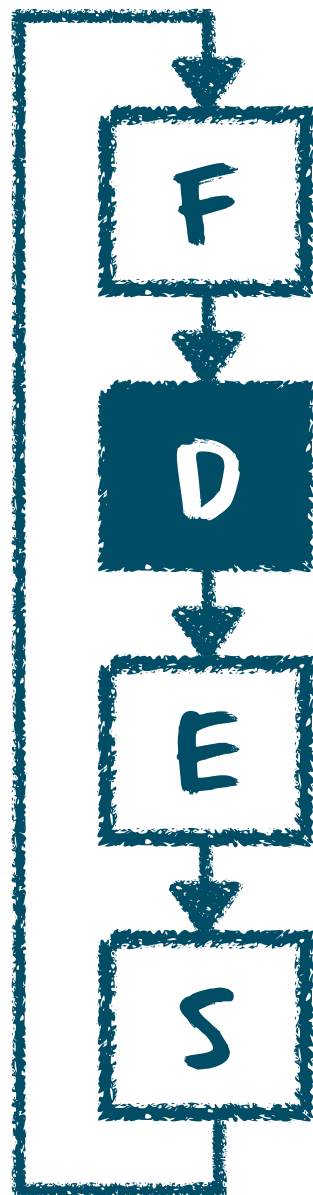


ALU: Arithmetic & Logic Unit

fetch instruction



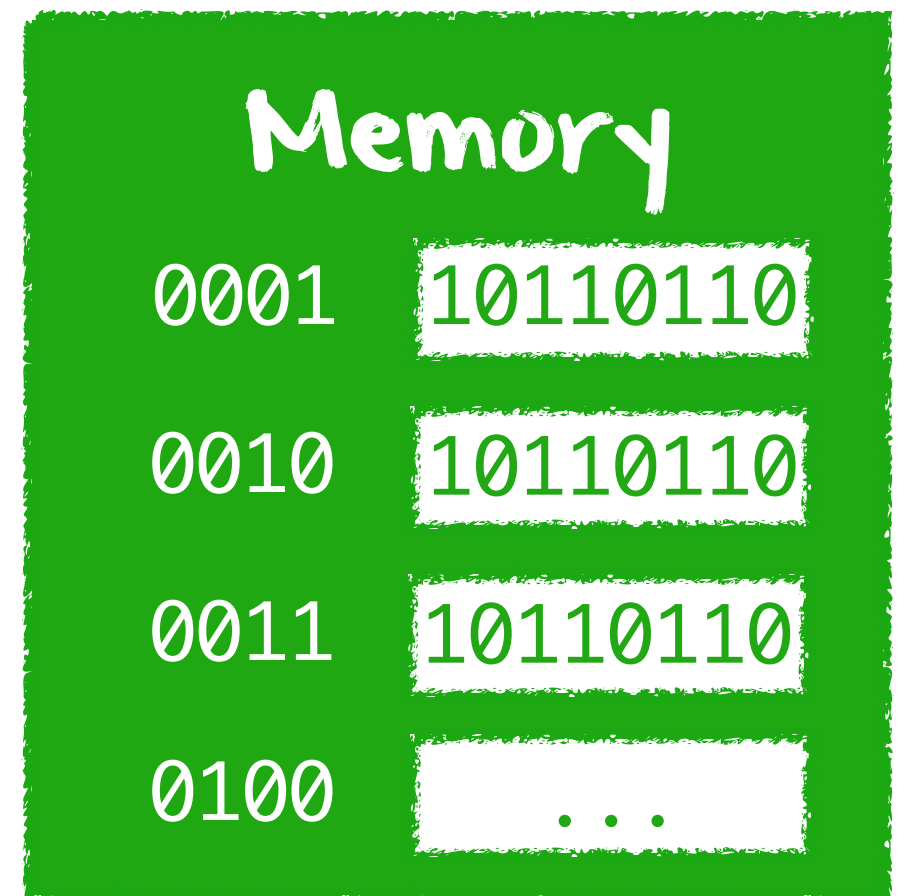
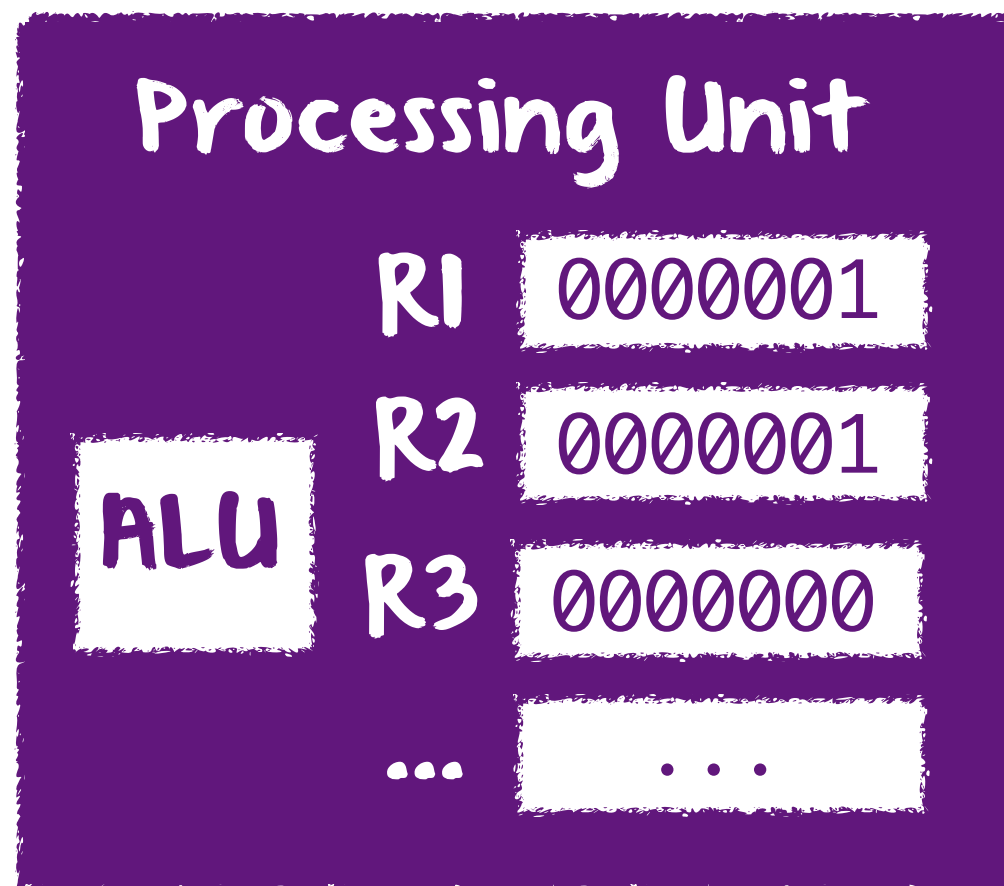
decode instruction



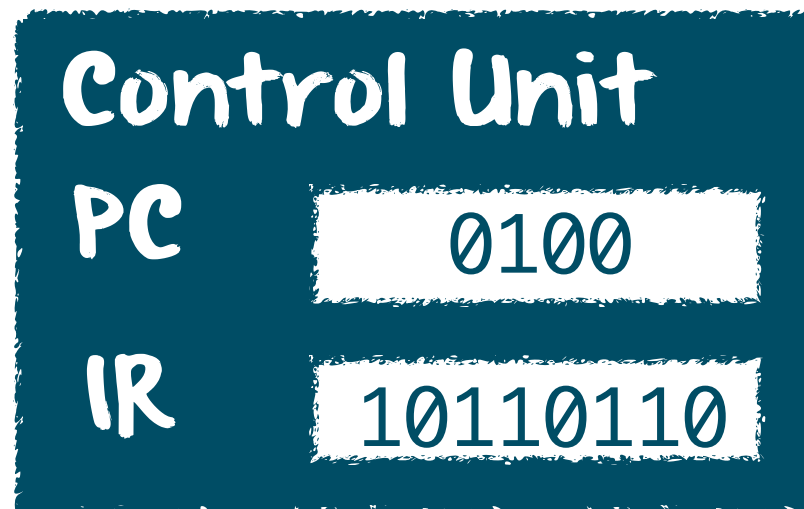
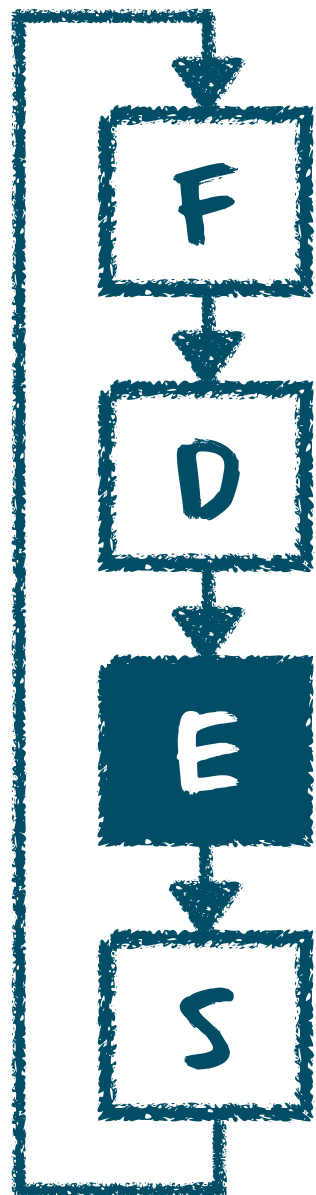
10 11 01 10

ADD R3 R1 R2

op dst src1 src2



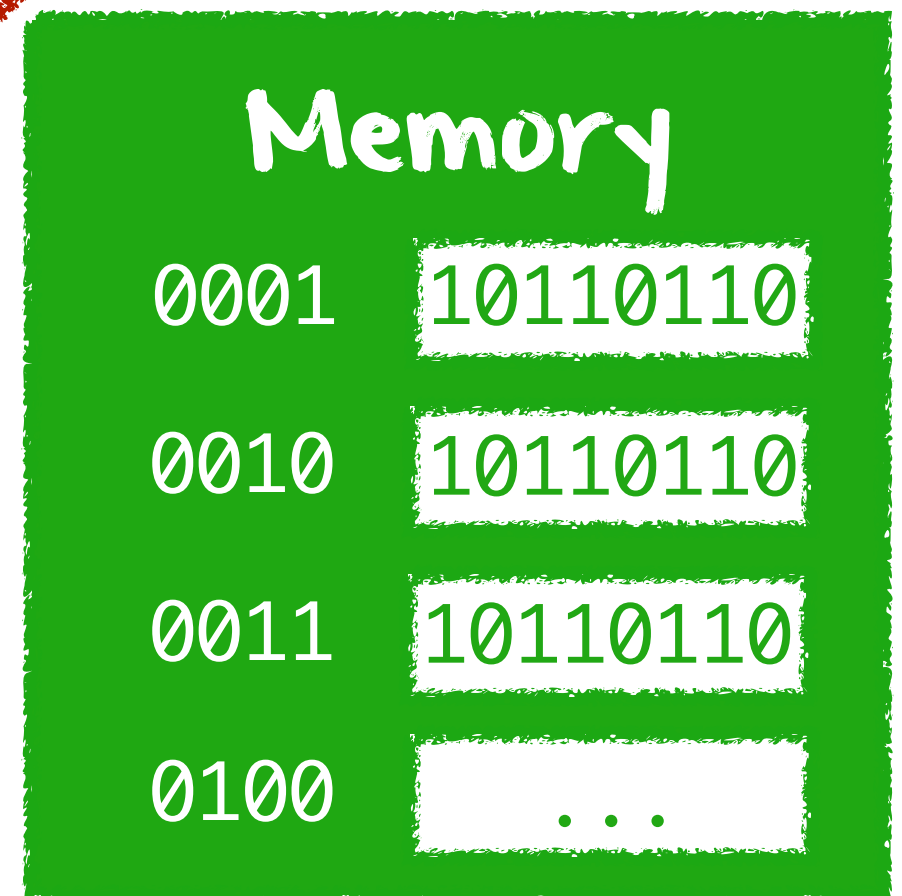
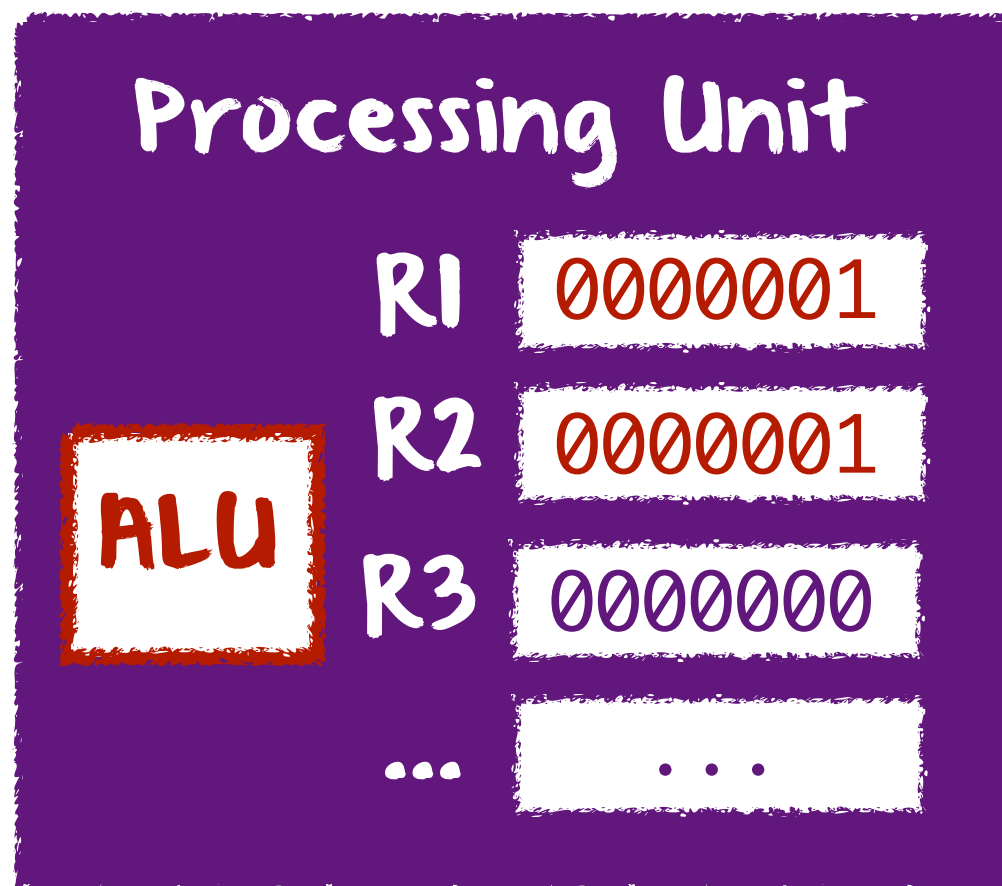
execute instruction



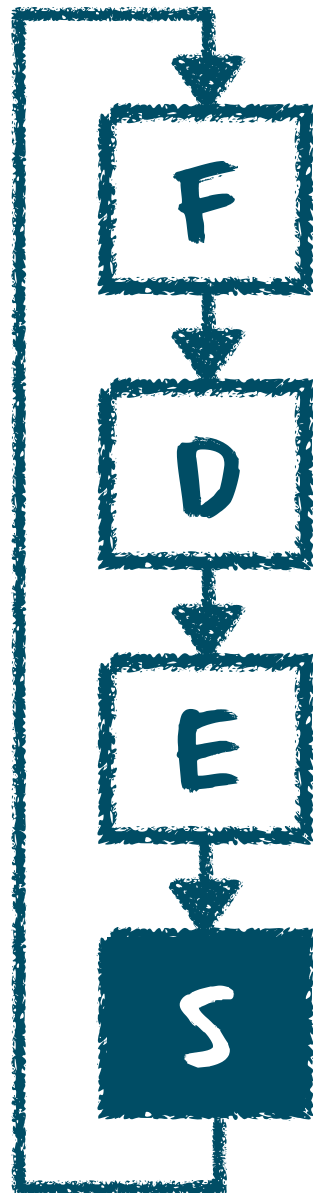
10 11 01 10

ADD R3 R1 R2

op dst src1 src2



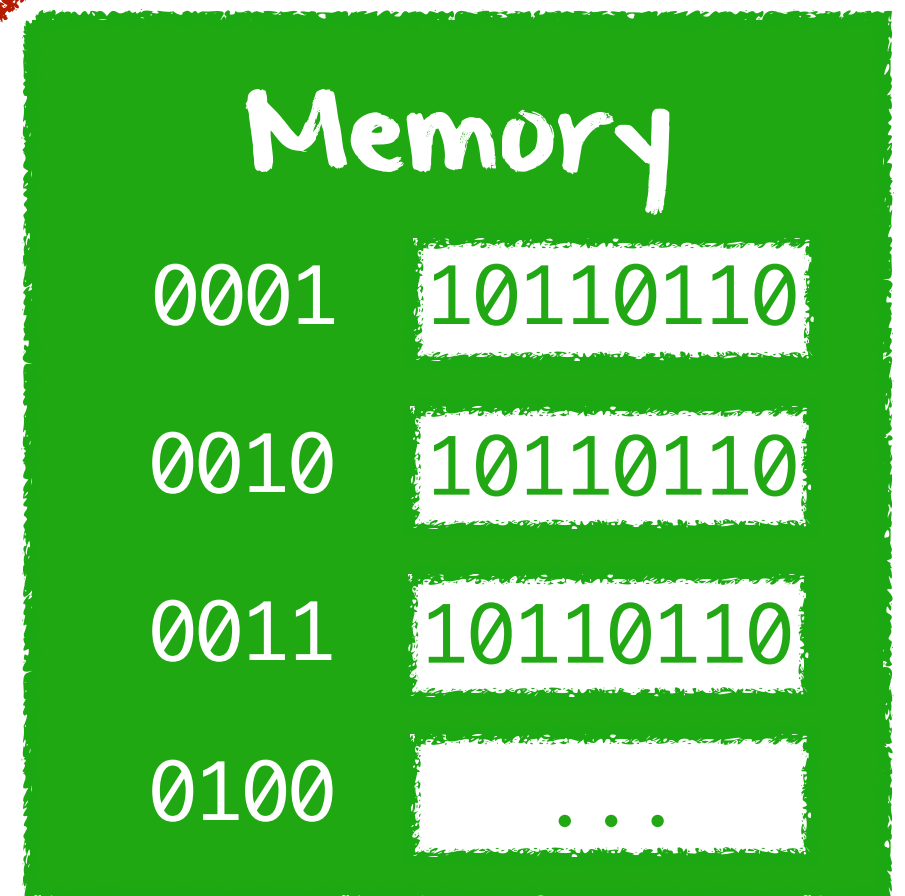
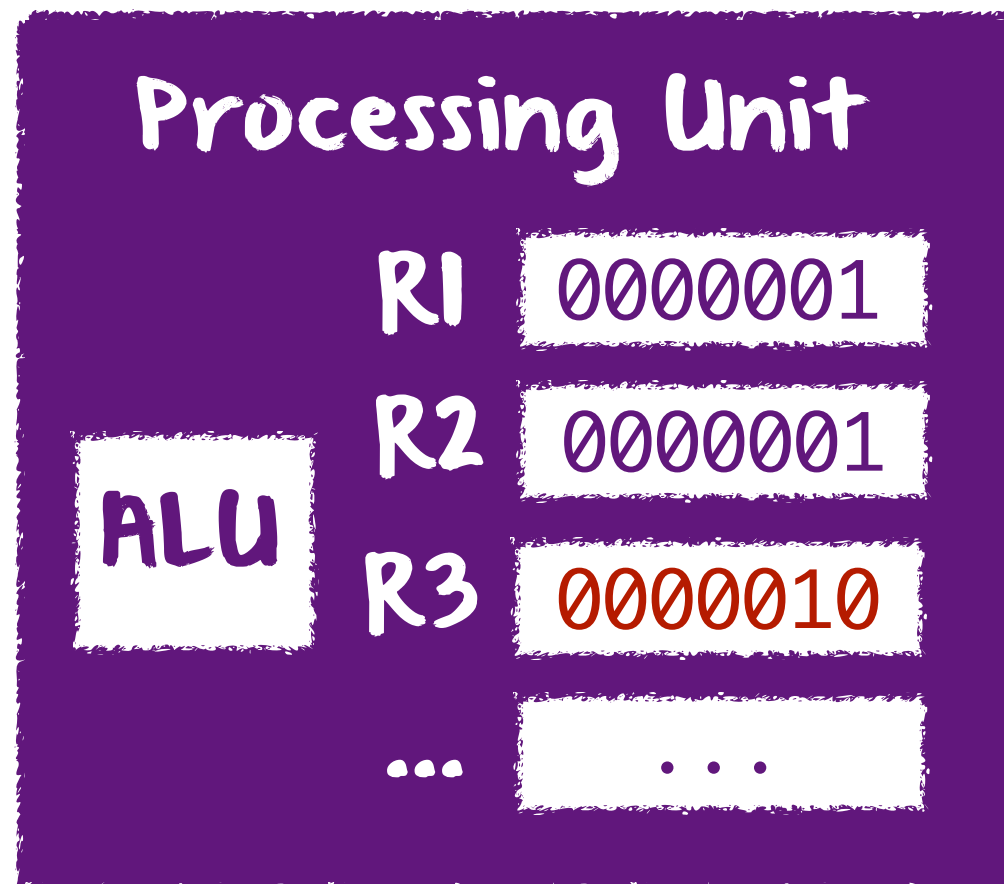
store result



10	11	01	10
----	----	----	----

ADD	R3	R1	R2
-----	----	----	----

op dst src1 src2



instruction sets

ADDSD—Add Scalar Double-Precision Floating-Point Values

Opcode	Instruction	64-Bit Mode	Compat/ Leg Mode	Description
F2 0F 58 /r	ADDSD <i>xmm1</i> , <i>xmm2/m64</i>	Valid	Valid	Add the low double-precision floating-point value from <i>xmm2/m64</i> to <i>xmm1</i> .

Description

Adds the low double-precision floating-point values from the source operand (second operand) and the destination operand (first operand), and stores the double-precision floating-point result in the destination operand.

The source operand can be an XMM register or a 64-bit memory location. The destination operand is an XMM register. The high quadword of the destination operand remains unchanged. See Chapter 11 in the *Intel® 64 and IA-32 Architectures Software Developer's Manual, Volume 1*, for an overview of a scalar double-precision floating-point operation.

In 64-bit mode, using a REX prefix in the form of REX.R permits this instruction to access additional registers (XMM8-XMM15).

Operation

$DEST[63:0] \leftarrow DEST[63:0] + SRC[63:0];$
(* DEST[127:64] unchanged *)

Intel IA-64
[2007]

Motorola 68000
[1980]

ADD

Add
(M68000 Family)

ADD

Operation: Source + Destination → Destination

Assembler Syntax: ADD <ea>, Dn
ADD Dn, <ea>

Attributes: Size = (Byte, Word, Long)

Description: Adds the source operand to the destination operand using binary addition and stores the result in the destination location. The size of the operation may be specified as byte, word, or long. The mode of the instruction indicates which operand is the source and which is the destination, as well as the operand size.

Condition Codes:

X	N	Z	V	C
*	*	*	*	*

X — Set the same as the carry bit.
N — Set if the result is negative; cleared otherwise.
Z — Set if the result is zero; cleared otherwise.
V — Set if an overflow is generated; cleared otherwise.
C — Set if a carry is generated; cleared otherwise.

Instruction Format:

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
1	1	0	1	REGISTER			OPMODE			EFFECTIVE ADDRESS MODE			REGISTER		